

Cardioid Challenge Questions

1. Describe the pattern that happens at the bottom of the image. Specifically, what happens at the vertices nearest $n/2$?
2. Explain why sometimes there is a line from top to bottom but not at other times.
3. Explain why, when $k = 2$, $n-1$ maps to $n-2$.
4. Explain the $n = k^2-1$, k image. In particular, why do 0 , $k+1$, $2k+2$, etc., all have empty spaces rather than one or more lines in and out?

FACT: The image when $n = 6$ and $k = 2$ has a square U with a vertical line in the middle like this:



5. For what other values of n do these same lines reappear (as part of the complete image)?
6. Suppose n is a multiple of 3, $n = 3j$ and $k = 2$. Verify that the BOTTOM of the cardioid envelope curve is $\frac{3}{4}$ of the way down the entire image. **HINT:** What are the coordinates of vertex j and $2j$ in this instance?