

Additional Image Detective Strategies

More **Things to notice** (beyond 1-10)

11. If you can see a structure that repeats itself, you may benefit by restricting the analysis to a portion of the image.

n is a multiple of the number of times it repeats itself.

12. If there are k levels of interior subdivision points shown, then S is likely $2k$ or $2k+1$. The reason is that the end of the first subdivision and the start of the last subdivision on a segment of the vertex frame are at the same level. The same goes for second and 2nd to last, and so on. Therefore

$S = 2$ and $S = 3$ produce a single level,

$S = 4$ and 5 produce 2 levels.

$S = 6$ and 7 produce 3 levels, and so on.

13. If you can count the number of segments in a structure that repeats itself, that provides an indication of S .

Consider the images to the right called Top, Middle, Bottom

a. Top repeats itself 5 times. Middle repeats itself 10 times and Bottom repeats itself 11 times.

b. (Green) The Top image has subdivision points at 3 levels.

This means S is likely 6 or 7 for Top. Counting the number of segments in $1/5$ of the whole is 7 so $S = 7$. Middle has 4 subdivision levels as does Bottom so both are $S = 8$ or 9. Counting from peak to peak confirms that $S = 8$ in Middle, but Bottom is harder to count that way.

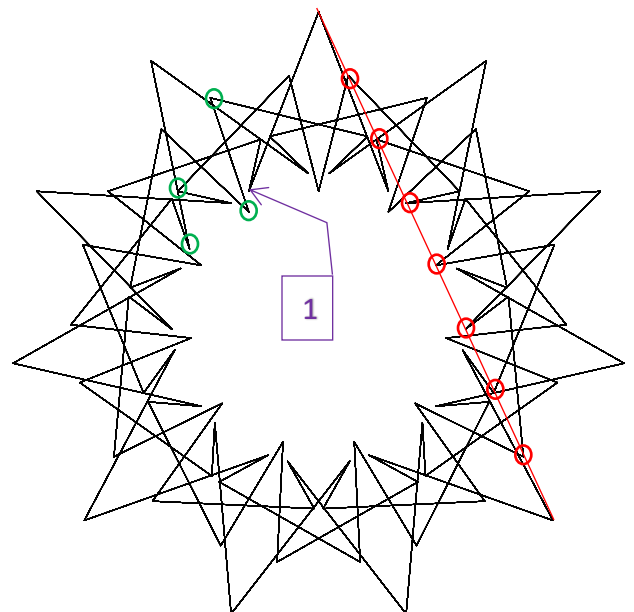
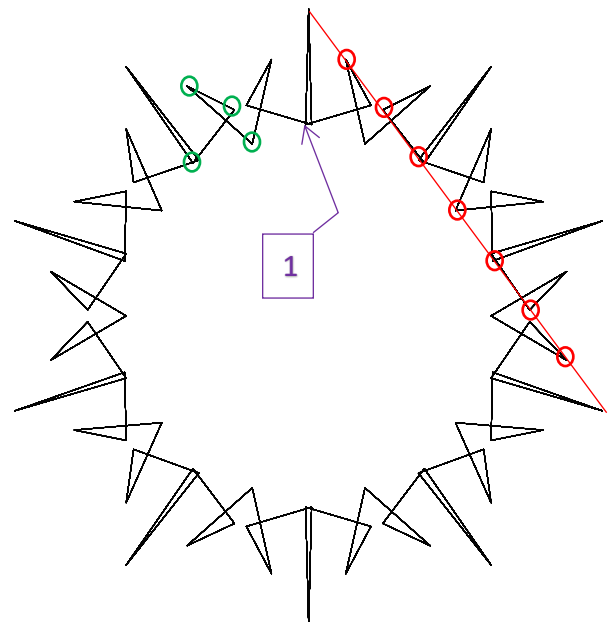
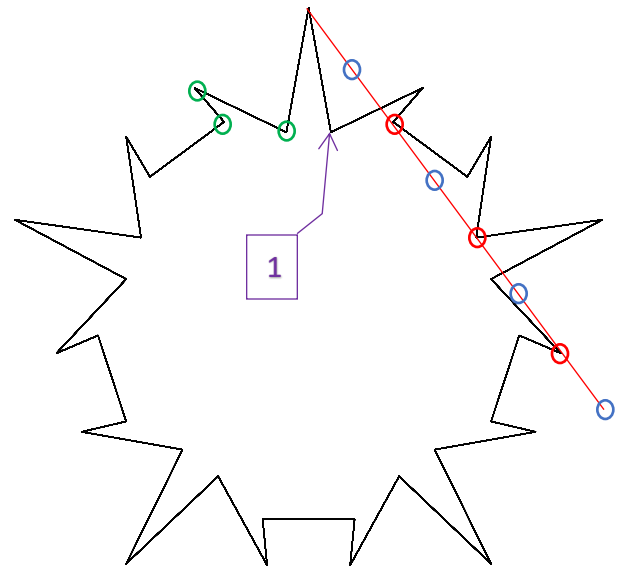
c. (Red) Checking the lines drawn for Top if $n = 5$ and $J = 1$ or 2 suggest that $n > 5$ must be true (as none of the internal vertices are on those lines). But $n = 10$, $J = 3$ coincides with all three levels of subdivisions. Note that these three points are **not** equally spaced on the line. This confirms that $S = 7$ for Top with subdivision endpoint not used noted in blue on this first line of the vertex frame.

By contrast, Middle and Bottom have a J that coincides with each level of the image so that $n = 10$, $J = 3$ for Middle and $n = 11$, $J = 4$ for Bottom. Equal spacing of subdivisions along first line of the vertex frame confirms that both images are $S = 8$.

Continue the vertex frame in each case to find P (labelled 1).

The 3rd subdivision on the 4th line of the vertex frame is the first point in the Top ($P = 24 = 3 \cdot 7 + 3$). The 3rd subdivision on the 4th line of the vertex frame is the first point in the Middle ($P = 27 = 3 \cdot 8 + 3$). Finally, the 3rd part of the 6th line of the vertex frame is the first point in the Bottom image ($P = 43 = 5 \cdot 8 + 3$).

Click below then click *Toggle Drawing* to see Bottom drawn.



<https://www.playingwithpolygons.com?vertex=11&subdivisions=8&points=43&jumps=4>