

On finding the smallest values of S , P , J , and n that creates an image

In order to make analysis easier, it is generally worthwhile to adjust parameters so that **VCF** and **SCF** are as small as possible and to decrease J and P so that they are as small as possible. It will not always be possible to have both **VCF** = 1 and **SCF** = 1, but it will make understanding how the image was created easier if you follow these suggestions. [Mathematically, **VCF** = $\text{GCD}(n, J)$ and **SCF** = $\text{GCD}(S*(n/\text{VCF}), P)$.]

An Example: Suppose you want to understand a bit more about the image at right. This was created by the *Initial* settings of $S = 8$, $P = 30$, $J = 9$ and $n = 15$. You would like to know how this was created.

In this instance, **VCF** = 3 and **SCF** = 10 so the first thing to do is to divide n and J by 3, and S and P by 2 giving $S = 4$, $P = 15$, $J = 3$ and $n = 5$. The same image emerges but now **VCF** = 1 and **SCF** = 5.

One cannot reduce n and P by the common factor of 5 without doing damage to the image ($n = 1$ results). But you can obtain the same image by making further adjustments to decrease the size of J and P .

Let $J = n - 3 = 2$ (since then J is, clockwise, less than half-way around), and similarly, $P = S*(n/\text{VCF}) - 15 = 5$. The *Final* version, $S = 4$, $P = 5$, $J = 2$ and $n = 5$, will be easier to count.

To see the difference, compare the two images from the companion website. Click **Show Subdivisions** and **Show Vertices** to obtain the images below. There are twice as many subdivision points and three times as many vertices on the left than the right.

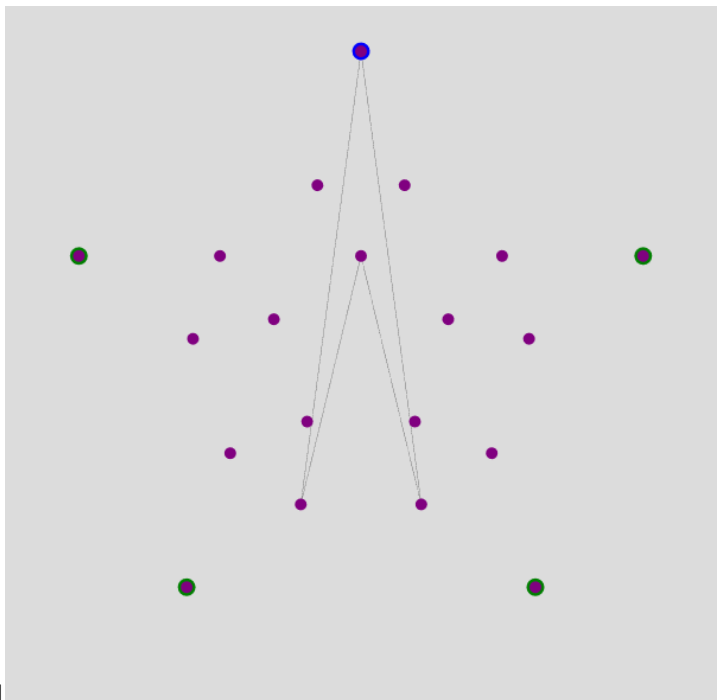
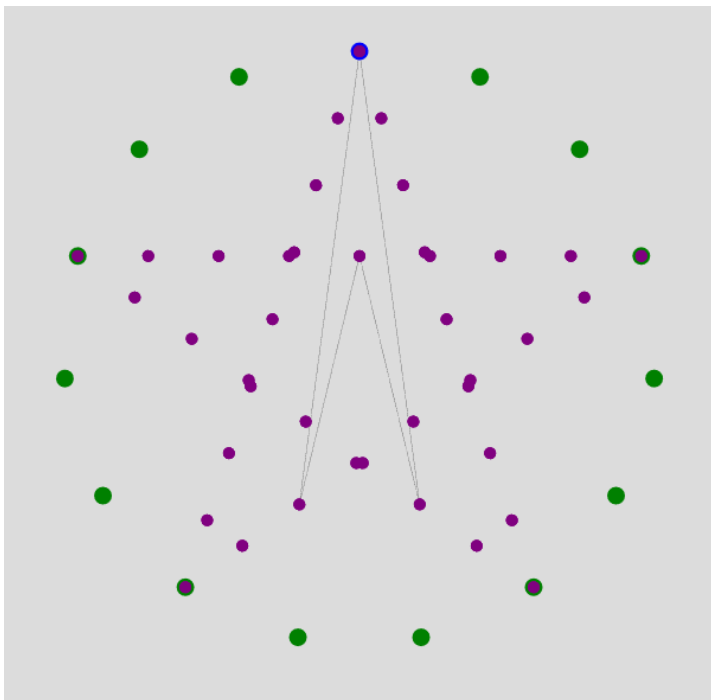
Initial, LEFT: <https://www.playingwithpolygons.com?vertex=15&subdivisions=8&points=30&jumps=9>

To draw the first line: The 30th subdivision (endpoint of the 1st segment) is on the 4th line of the vertex frame since $30 = 3*8+6$. The first 3 segments of the vertex frame go from vertex 0 to 9 to 3 to 12 and the 6th subdivision point on the line going from vertex 12 to vertex 6 is the endpoint of the first segment in the final image.

Final, RIGHT: <https://www.playingwithpolygons.com?vertex=5&subdivisions=4&points=5&jumps=2>

To draw the first line: The 5th subdivision (endpoint of the 1st segment) is the first subdivision on the second line segment since $5 = 1*4+1$. The first vertex frame segment goes from vertex 0 to 2 and the second goes from 2 to 4.

Both methods produce the same image, but the one on the right is easier to follow.



1/3 of vertices used (**VCF**=3) & 1/10th subdivisions (**SCF**=10) | All vertices used (**VCF**=1) & 1/5th subdivisions used (**SCF**=5)

