

Subdivision Patterns and what this implies about S and P for Centered-Point Flowers

The simplest extension of jump patterns is to simply **Jump** one vertex ($J = 1$) then **In** to the center, C , and back **Out** to the same vertex. Each move like this carries with it S subdivisions so the image shown is unlike other files in that the center is explicitly included in each jump set. Each vertex of the n -gon gets used twice. Given the $n = 3$ vertex frame discussed in the [Jumps Primer](#), this creates the following subdivision endpoints (noted beneath the vertex and center jumps):

$$0 \text{ to } 1 \text{ to } C \text{ to } 1 \text{ to } 2 \text{ to } C \text{ to } 2 \text{ to } 3 \text{ to } C \text{ to } 3$$

$$S \quad 2S \quad 3S \quad 4S \quad 5S \quad 6S \quad 7S \quad 8S \quad 9S$$

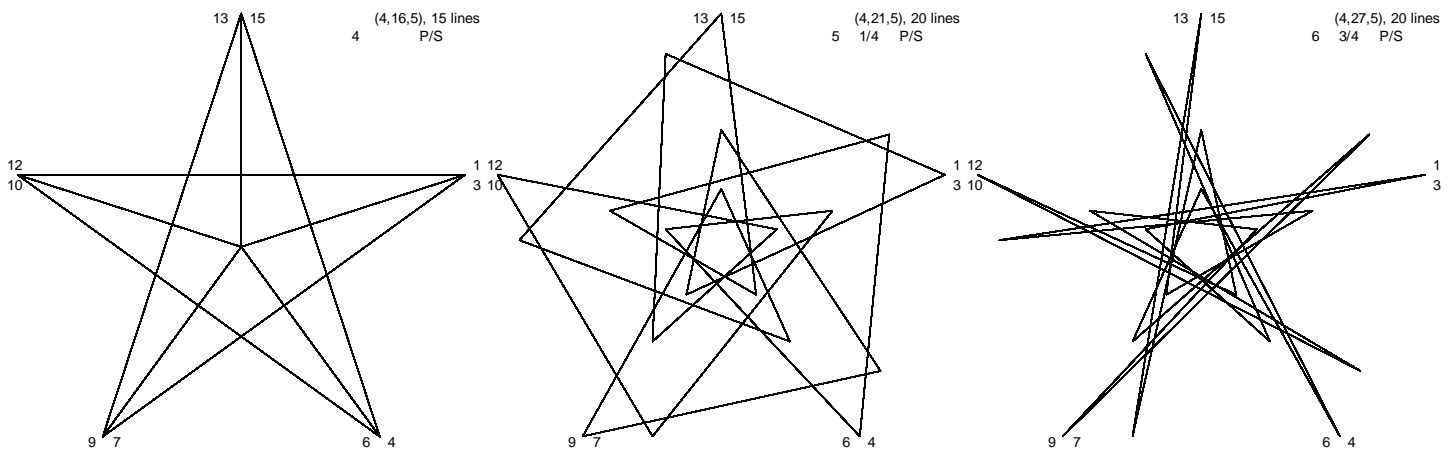
Because of the “**Jump, In, Out**” pattern, each new vertex involves three moves. Notice in particular that the following is true about the multiple, m , in front of S in each case:

Jump If this is the first time vertex v is used, then $m = 3v - 2$ ($m = 1$ if $v = 1$, $m = 4$ if $v = 2$, and $m = 7$ if $v = 3$).

In The move **into the center** is always of the form: $m = 3v - 1$ ($m = 2$ if $v = 1$, $m = 5$ if $v = 2$, and $m = 8$ if $v = 3$).

Out The move back **out from the center** to v is of the form: $m = 3v$ ($m = 3$ if $v = 1$, $m = 6$ if $v = 2$, and $m = 9$ if $v = 3$).

This same pattern works for values n beyond $n = 3$, for each vertex v of the n -gon, $1 \leq v \leq n$, as we see for $n = 5$ below.



These five “pentagrams with attitude” based on $n = 5$ and $S = 4$ are each annotated with multiple values m noted above (together with P/S which tells us where the first line lands relative to these multiples of S vertices). Each is more pentagram like than pentagon like because $4 \leq P/S < 7.5 = 3n/2$ (half-way around). You should be able to see where the first line ends in each image. Remember that $m = 5$ and 8 are at the center so the top middle $5 \frac{1}{4}$ is $1/4^{\text{th}}$ of the way out from the center 5 to $m = 6$ at vertex 2 (and the top left first 4 lines in terms of m are $4-8-12-1$ since $16-15 = 1$). The top 3 have fewer lines because $SCF > 1$. The bottom right is a *porcupine* ($P = 31$ is the same image and $P = 30$ is a single line).

