## Centered-Point Flower Images when $\boldsymbol{P}$ is a multiple of $S$

In the traditional string art model, the image is a polygon or star whenever $\boldsymbol{P}$ is a multiple of $\boldsymbol{S}, \boldsymbol{P}=\boldsymbol{m} \cdot \boldsymbol{S}$. This is not always true with Centered-Point Flowers. We focus on $\boldsymbol{n}=11$ and 12 in order to see what differences emerge when $\boldsymbol{n}$ is prime versus composite. Instead of being exhaustive with images, this explainer examines some of the general patterns that are laid out in the table showing what happens given $\boldsymbol{m} \leq 3 \boldsymbol{n} / 2$. (Note: $\boldsymbol{P}=\boldsymbol{m} \cdot \boldsymbol{S}$ implies SCF $=\boldsymbol{S}$ so there are $3 \boldsymbol{n}$ possible lines regardless of $\boldsymbol{S}$. These images use $\boldsymbol{S}=1$, so $\boldsymbol{P}=\boldsymbol{m}$.)

Images are symmetric across $3 \boldsymbol{n} / 2$. To put it another way, $\boldsymbol{m}$ and $3 \boldsymbol{n}-\boldsymbol{m}$ produce the same static image, with the only difference being the way in which the image is drawn.

When $\boldsymbol{n}$ is prime, all polygons and stars with and without rays are represented. The only unusual image occurs at $\boldsymbol{m}=11, \mathrm{SCF}=11$. This produces the obtuse triangle at left below that goes from 11-gon vertices 11\&0-Center-8-11\&0 (the 3 lines end at $\boldsymbol{P}=11,22,33$ ).

When $\boldsymbol{n}$ is composite, some $\boldsymbol{n}, \boldsymbol{J}$-stars that are not possible without rays, are possible with rays (such as those associated with $\boldsymbol{m}=7,10,11$, and 14). Note however that one cannot draw a 6,2 or 12,3 star without using the center. Instead, one obtains a triangle ( $\boldsymbol{m}=12$ )

| $m$ | $n=11$ |  | $n=12$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Image* | $3 n-m$ | Image | $3 n-m$ |
| 1 | $V \mathrm{~F}=11 \mathrm{RP}$ | 32 | $V F=12 \mathrm{RP}$ | 35 |
| 2 | 11 R | 31 | 6 R | 34 |
| 3 | 11 P | 30 | 12 P | 33 |
| 4 | 11,2 RS | 29 | $3 \mathrm{Tv.1}$ | 32 |
| 5 | $\mathrm{VF}=11 \mathrm{RP}$ | 28 | VF = 12 RP | 31 |
| 6 | 11,2 S | 27 | Hexagon | 30 |
| 7 | 11,3 RS | 26 | 12,3 RS | 29 |
| 8 | 11,2 RS | 25 | $3 \mathrm{Tv}$. | 28 |
| 9 | 11,3S | 24 | Square | 27 |
| 10 | 11,4 RS | 23 | 6,2 RS | 26 |
| 11 | Obtuse $\Delta$ | 22 | 12,3 RS | 25 |
| 12 | 11,4S | 21 | Triangle | 24 |
| 13 | 11,5 RS | 20 | 12,5 RS | 23 |
| 14 | 11,4 RS | 19 | 6,2 RS | 22 |
| 15 | 11,5 S | 18 | 12,5 S | 21 |
| 16 | 11,5 RS | 17 | 6 R | 20 |
| 17 |  |  | 12,5 RS | 19 |
| 18 |  |  | Vertical | 18 |

*Acronyms: \#,\#\# n,J-star; P-polygon; R-rays; RS-star with rays; S-star; T-equilateral triangle; VF-Vertex Frame. BOLD images are shown below. or square $(\boldsymbol{m}=9)$ since $12 \cdot 3=9 \cdot 4=36=3 \boldsymbol{n}$. The mirror-image 3 equilateral triangles, $\boldsymbol{m}=4$ and $\boldsymbol{m}=8$, are shown below.

Each ribbed star is drawn twice in the table (and twice more for $m>3 n / 2$ ). The bottom two images are sharpest ribbed stars, 11,5 and 12,5 , both of which can be drawn with $\boldsymbol{m}=13$.


13
P/S
( $1,11,11$ ), 3 lines, 11 SCF



