

A Counting Squares Challenge Question

This image is the VF from the zig-zag [truncated pentagrams](#) image sequence discussed [here](#), if the original $n = 25$ is changed to $n = 20$, in which case, $VCF = 5$ so the image has 90° rotational symmetry and there are 240 900-line images in the [new image sequence](#). This VF has a number of rectangles as a result but some of them are also squares. The question is: **How many squares are in the image?**

3 Hints: **1.** You should be able to see a 5×5 square in this image (connecting vertices 3, 8, 13, and 18) so certainly that is included. But there 3×3 , 2×2 and 1×1 squares that also must be counted. **2.** To avoid double counting, you should start by noting a “distinguished vertex” (you have four choices here: lower left, lower right, upper left or upper right) and only count based on that. **3.** To be a square, at least one of the opposing sides must have opposing vertices that are on a diagonal of the 20-gon (i.e., on one of the lines connecting vertex a to vertex $a+10$ for $0 \leq a < 10$) which in this case means on 3-13 or 8-18.

