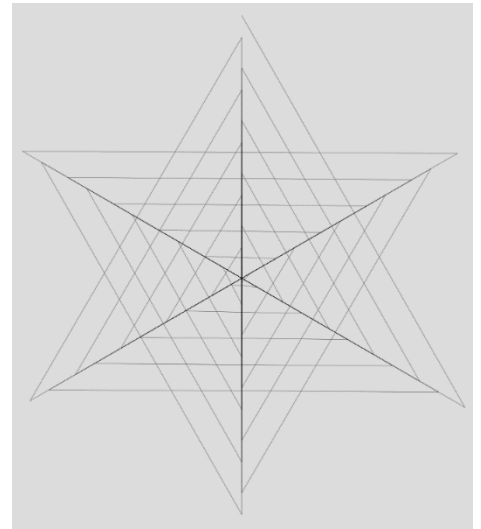


An Introduction to Jump Sets

Jump sets can be employed to create variations on spirals, just like they were used in Part III of ESA. [E16.2](#) introduced jump sets to create a 6,2-star by alternating jumps of 2 and 3 on a 6-gon. The vertex frame, VF, for that star shown to the left is created in 12 lines connecting vertices **0-2-5-1-4-0-3-5-2-4-1-3-0**. [E2.2.1](#) notes why $n = 6$ is the only value of $n > 4$ for which one could not produce at least one n -point *continuously drawn* star via a single-jump model.



The image to the right is a spiral version of a 6,2-star based on this same jump set of 2 then 3. Like all spirals (without mirror clicked on), the image on the right has no line of symmetry. Nonetheless, it appears quite similar to the 6,2-star achieved via web mirror with horizontal line of symmetry discussed [elsewhere](#).

When $n = 12$ we can talk in terms of hours (with $12 = 0$). The string-art VF at bottom left is based on a jump set of (1,10). It is counterclockwise drawn (the first 5 lines of the VF are 0-1-11-0-10-11-...) but it could have been created three other ways. Switching the first and second jump to (10,1) maintains the counterclockwise drawn nature of the image since the first 5 lines are then 0-10-11-9-10-8-... . Subtracting n from each jump (for jump set pairs of (11,2) and (2,11)) produces images drawn clockwise since the first 5 lines of (11,2) are 0-11-1-0-2-1-... , and the first 5 lines of (2,11) are 0-2-1-3-2-4-... . In the spirals context, each produces a different image because the order of radius reduction changes.

The [first](#) and [second](#) shown above are counter-clockwise, \curvearrowright . The [third](#) and [fourth](#) shown below are clockwise, \curvearrowleft . (Compare to these [n=12, J=11](#) \curvearrowright and [n=12, J=1](#) \curvearrowleft single-jump versions.)

All four highlight the first 24 lines (which is how many lines are required to complete the string-art VF below). All four spirals are 5-times around because $r = 120 = 5 \cdot 24$.

