## **Even Spiderwebs and Odd Foghorns**

When n is even, a jump of n/2 as part of a jump set creates sharp lines through the center of the parent polygon. When the other jump is 1 or n-1 the spiral images that result resemble foghorns or spiderwebs depending on whether n is divisible by 2 but not 4 of if n is divisible by 4. It is convenient to have the first jump be n/2 and the second be 1.

An aside on missing pieces of the pie. The double jump model in Chapter 16 of ESA included multiple versions of the double jump *Excel* file. As discussed in E16.5, one version reversed direction for the last half of the string art image to fill in the missing pieces when n = 4k+2. The vertex frame, VF, to the left shows the issue for n = 6. Given this jump set pattern, the VF is completed after n or 6 jumps: 0-3-4-1-2-5-0. If this is filled in in a string-art fashion, there will be n/2 = 3 petals in the flower like the second image, or n/2 = 3 pieces of pie, not 6. By contrast when n = 4k like n = 8, the VF is completed after 2n or 16 jumps: 0-4-5-1-2-6-7-3-4-0-1-5-6-2-3-7-0 and the flower has  $n = \frac{8 \text{ petals}}{2}$  or n = 8 pieces of pie like the last two images. This pattern continues for larger n, half the pieces are missing if n = 4k+2, all are there if n = 4k.



Odd spiral foghorns and even spiderwebs. If n = 4k+2 there are 2k+1 (an odd number) of foghorns (the other sections are open) like n = 6, 10, 14 from L-R. If n = 4k, all 4k sections are filled in and spiderwebs result like n = 8, 12, 16 below.

