Sharpest Even Isosceles Triangles Images – Challenge Questions



The four columns represent four types of sharpest isosceles triangles on even polygons images, two with horizontal base and two with slanted base. The first and third are n = 4k images and the second and fourth are n = 4k+2 images. The first row shows k = 2 and the second shows k = 3. (k = 1 images (so n = 4 or 6) are possible but are less interesting from the perspective of seeing pattern development and are left to the reader because k = 1 produces isosceles right triangles and equilateral triangles images rather than sharpest apex triangles images.) What are general formulas for the number of triangles, T, for each type of image?

1. $T_{\underline{H}}(n = 4k)$ 2. $T_{\underline{H}}(n = 4k+2)$ 3. $T_{S}(n = 4k)$ 4. $T_{S}(n = 4k+2)$

3 Hints. *i*. These 8 images have been copied to a separate sheet of the *Sharpest Isosceles Triangles Excel* file to facilitate apex mark ups as described at the start of this chapter. *ii*. If you want to check your equations without looking in Chapter 20, k = 7 values are: n = 28, 1. 254, 3. 266; and n = 30, 2. 308, 4. 294. *iii*. If you prefer to use the *General Triangles* file, set j = INT((n-1)/2), k = j+2, v = 1, w = n-1 for horizontal images, and j = INT(n/2), k = j+2, v = 2, w = n-1 for slanted images.